



Explanation of the Rpgt Technique-Based Reliability and Availability Analysis System

Sanju Kumari, Research Scholar, Department of Mathematics, Baba Mastnath University Asthal Bohar, Rohtak, Haryana, India. Email: sanjusheoran1993@gmail.com
Dr. Sangeeta Malik, Professor, Department of Mathematics, Baba Mastnath University Asthal Bohar, Rohtak, Haryana, India. Email: sangeeta@bmu.ac.in
Dr. Jai Bhagwan, Assistant Professor, Department of Mathematics, Govt P. G. Nehru College, Jhajjar, Haryana, India. Email: jaichaudhary81@gmail.com

Abstract

In the present paper, reliability analysis is examined for consistent state. The Processing/Manufacturing industry is isolated into numerous subsystems. Subsystems are either in parallel/equal or in arrangement. Taking failure and repair rates constant. The subsystem may flop totally through partial disappointment. At the point when any subsystem flops then the framework is in bombed state. A state diagram of system portraying the transition rates is drawn. Articulations for way probabilities mean sojourn times, MTSF, availability, busy period of the server and expected no. of server's visits are inferred utilizing RPGT. Behaviour analysis of the framework is done. Graphs are prepared to compare and draw the conclusion.

Keywords: Rpgt, Mtsf, Availability

1. Introduction:

Reliability optimization is a tremendous area in area of reliability engineering that has improved much more factor in the posting in the last 100 years. Toward the start, it was attached to correspondence as well as information systems. The fundamental target of this particular work is improving system Reliability; it is characterized to become the chance that the device works properly in any case up to a predetermined time-frame (i.e., the mission time) beneath expressed problems. Due to the multifaceted dynamics of devices like a broad rule, the results of the inconsistent conduct of theirs have ended up to be serious so far as price, effort, etc. Consequently, in getting on the method reliability and moreover the basic need for growing the reliability of products as well as product have ended up to be progressively more vital to the exploration system. Most of assets in sector are repairable methods. The demonstration of those assets is able to affect the quality of merchandise, the expense of occupational, the assistance of the buyers, moreover along these directions the gain of endeavors straightforwardly. The researchers have talked about the reliability and accessibility of numerous stochastic systems and processing industry by utilizing awkward and time-consuming techniques. Jieong et al. (2009) used GA, or a half-and-half calculation, to address multi-objective streamlining problems. The fundamental objective of the paper by Kumar et al. (2019) focuses on the investigated examination of the washing element in the paper company consuming RPGT, while Kumar et al. (2017) analyzed the urea compost industry for system parameters. In their 2018 study, Kumar et al. focused on the investigation of a bakery and an edible petroleum treatment plant. In a series framework with a span portion, Bhunia et al. (2010) presented GA to address concerns with unshakable quality stochastic augmentation. The review found a solution to the problem of streamlining stochastic unshakable quality in light of the series framework's chance imperatives. The mist group of a coal-fired thermal impact shrub was optimized by Malik et al. in 2022. Dual categories of deficiencies—simple and hard as for the time in which these happen for disengagement and expulsion following their recognition—have been reported in Anchal et al.(2021) .'s analysis of the SRGM classic using variance condition. Komal et al. (2009) described the reliability, availability, and maintainability analysis presents some strategies to carryout structure alteration. Benefit analysis of the agribusiness harvester plants in a stable



condition using RPGT was discussed by Kumari et al. in 2021. Goel, P., Goyal, V., Kumar, A., Singh J. what's more, numerous others, have examined and talked about systems under consistent state conditions, utilizing the accompanying formulae of the RPGT to find the key parameters of a stochastic system:

- a) MTSF
- b) Availability
- c) Server of the busy period
- d) Expected number of server's visits/replacements

2. ASSUMPTIONS AND NOTATIONS:-

The following assumptions and notations/symbols are used:

- 1) There is a single repair facility catering to the needs of three units as and when need arises.
- 2) The distribution of the failure & repair times are exponential and general respectively and also different for three units.
- 3) They are also assumed to be independent of each other.
- 4) Repairs are perfect i.e. the Repair facility never does any damage to the units.
- 5) A Repaired unit works like a new one.
- 6) The system is down if any one of the unit fails completely.
- 7) Nothing can fail further when the system is in failed state.
- 8) The system is discussed for steady state conditions.

pr / pf : Probability/transition probability factor.

$q_{i,j}(t)$: probability density function (p.d.f.) of the first passage time from a regenerative state i to a regenerative state j or to a failed state j without visiting any other regenerative state in $(0,t]$.

$p_{i,j}$: Steady state transition probability from a regenerative state i to a regenerative state j without visiting any other regenerative state. $p_{i,j} = q_{i,j}^*(0)$; where $*$ denotes Laplace transformation.

cycle: A circuit formed through un-failed states.

k-cycle: A circuit (may be formed through regenerative or non-regenerative/failed states) whose terminals are at the regenerative state k .

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$(i \xrightarrow{sr} j)$: r -th directed simple path from i -state to j -state; r takes positive integral values for different paths from i -state to j -state.

$(\xi \xrightarrow{fff} i)$: A directed simple failure free path from ξ -state to i -state.

$V_{k,k}$: pf of the state k reachable from the terminal state k of the k -cycle.

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$R_i(t)$: Reliability of the system at time t , given that the system entered the un-failed regenerative state i at $t=0$.

$A_i(t)$: Probability that the system is available in up-state at time t , given that the system entered regenerative state i at $t=0$.

$B_i(t)$: Probability that the server is busy doing a particular job at epoch t , given that the system entered regenerative state i at $t=0$.

$V_i(t)$: The expected number of visits of the server for a given job in $(0,t]$, given that the system entered regenerative state i at $t=0$.

$W_i(t)$: Probability that the server is busy doing a particular job at epoch t without transiting to any other regenerative state 'i' through one or more non-



- regenerative states, given that the system entered the regenerative state 'i' at t=0.
- μ_i : Mean sojourn time spent in state i, before visiting any other states;

$$\mu_i = \int_0^{\infty} R_i(t) dt$$
- μ_i^1 :The total un-conditional time spent before transiting to any other regenerative states, given that the system entered regenerative state 'i' at t=0.
- η_i :Expected waiting time spent while doing a given job, given that the system entered regenerative state 'i' at t=0; $\eta_i = W_i^*(0)$.
- f_j :Fuzziness measure of the j-state.
- λ/λ_1 :Constant failure rate of the main operative unit/the redundant unit.
- G(t)/g(t) :Probability density function/cumulative distribution function of the repair-time of the operative unit.
- H(t)/h(t) :Probability density function/cumulative distribution function of the repair-time of the redundant unit.
- α : Direct continuous failure rate of main unit A to α
- α_1 : Failure rate of unit A to reduced state \bar{A} .
- α_2/ β_2 : Failure/repair rate of unit A since reduced/failed state
- α_3/ β_3 : Failure/repair rate of server S
- α_4/ β_4 : Failure/repair rate of standby unit B.
- A/ \bar{A} /a: Unit in complete capacity operational / reduced / failed state. B/(B)/b: Unit B is good online /cold standby /failed mode.
- S/s: server in good/failed state

3. TRANSITION DIAGRAM OF THE SYSTEM

Following the above assumptions and notations, the transition diagram of the system is shown in fig.1

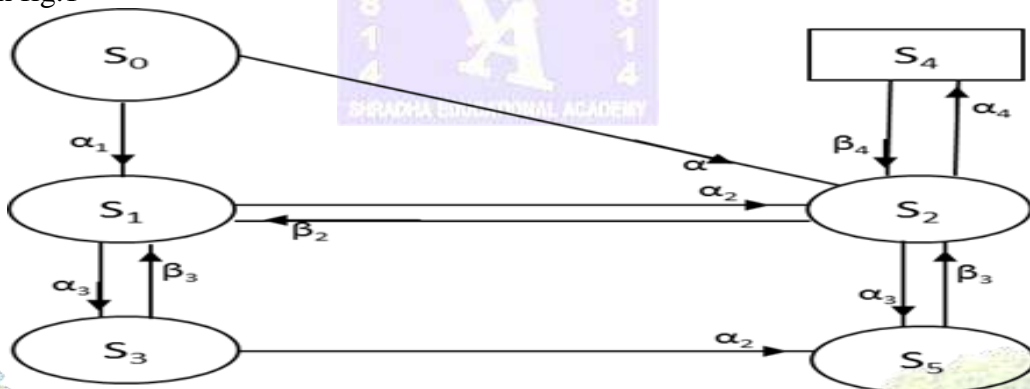


Figure 1: Transition Diagram

4. METHODOLOGY

Regenerative Point Graphical Technique:

4.1 Mean Time to System Failure:

$$MTSF = \left[\sum_{i, S_r} \left\{ \frac{\{pr(\xi^{S_r(sff)} \rightarrow i)\} \cdot \mu_i}{\prod_{k_1 \neq \xi} \{1 - V_{k_1, k_1}\}} \right\} \right] \div \left[1 - \sum_{S_r} \left\{ \frac{\{pr(\xi^{S_r(sff)} \rightarrow \xi)\}}{\prod_{k_2 \neq \xi} \{1 - V_{k_2, k_2}\}} \right\} \right]$$

4.2 Availability:

$$A_0 = \left[\sum_{j, S_r} \left\{ \frac{\{pr(0^{S_r})\} \cdot f_j \cdot \mu_j}{\prod_{k_1 \neq 0} \{1 - V_{k_1, k_1}\}} \right\} \right] \div \left[\sum_{i, S_r} \left\{ \frac{\{pr(0^{S_r})\} \cdot \mu_i^1}{\prod_{k_2 \neq 0} \{1 - V_{k_2, k_2}\}} \right\} \right]$$

4.3 Server of busy period:



$$B_{\xi} = \left[\sum_{j, Sr} \left\{ \frac{\{pr(\xi \rightarrow j)\} \cdot \eta_j}{\prod_{k_1 \neq \xi} \{1 - V_{k_1, k_1}\}} \right\} \right] \div \left[\sum_{i, Sr} \left\{ \frac{\{pr(\xi \rightarrow i)\} \cdot \mu_i^1}{\prod_{k_2 \neq \xi} \{1 - V_{k_2, k_2}\}} \right\} \right]$$

4.4 The number of the Server's visits/Replacements:

$$V_{\xi} = \left[\sum_{j, Sr} \left\{ \frac{\{pr(\xi \rightarrow j)\}}{\prod_{k_1 \neq \xi} \{1 - V_{k_1, k_1}\}} \right\} \right] \div \left[\sum_{i, Sr} \left\{ \frac{\{pr(\xi \rightarrow i)\} \cdot \mu_i^1}{\prod_{k_2 \neq \xi} \{1 - V_{k_2, k_2}\}} \right\} \right]$$

5. CONCLUSION:

The Regenerative-Point Graphical Technique is useful for the evaluation of the parameters in a simple way, without writing any state equation and without doing any lengthy and cumbersome calculations. This study can be extended to time dependent case. As it is easy for the management to control repair rates in comparison to failure rates, fixing the target of availability repair rates can be determined and managed by having efficient server.

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